**Topic: Mixed Applications of Networks**

Time: 45 mins Marks: /45 marks

**No calculator allowed**



**Question One: [4, 2: 6 marks]**

a) Find the maximum flow of the network below.

b) Show that the maximum flow is equal to the minimum cut.

**Question Two: [4, 2, 2, 3, 2: 13 marks]**

Borat is planning his next holiday. Once he has decided that he wants to go on holiday the following things need to happen before he can go.

|  |  |  |
| --- | --- | --- |
| **Activity** | **Preceding activity** | **Time to complete activity** |
| Pick a destination | None | 2 weeks |
| Get relevant vaccinations and health checks | Pick a destination | 3 days |
| Apply for passport | Pick a destination | 6 weeks |
| Start saving money | Pick a destination |  |
| Apply for a visa | Apply for a passport | 2 weeks |
| Travel insurance | Get relevant vaccinations and health checks | 3 days |
| Buy a plane ticket | Start saving | 1 day |
| Change currency | Buy a plane ticket | 1 day |
| Pack suitcase | Travel insurance, Apply for visa, Change currency | 2 days |
| Go to the airport and get on plane | Pack suitcase | 1 day |

a) Add the information from the table to the project network below, complete the project network and calculate the number of days Borat allocated to saving money if it takes 100 days before he leaves for his holiday.

 [Note: The diagram below is not drawn to scale]

b) What is the latest possible day he can start getting his health checks and vaccinations without delaying leaving for his holiday?

After deciding where is going to travel to Borat begins collecting donations to take to an orphanage in a village he will visit.

c) How long can be collect donations for without it delaying his departure?

d) If Borat finishes all his relevant health checks on July 14th and uses all the float time allowed for this activity, what date does he go to the airport to get on the plane?

e) If there is a delay in the processing of his visa application and it takes an extra four weeks to process, how does this affect how long it takes before he can leave for his holiday?

**Question Three: [3, 3, 3: 9 marks]**

Michael is having trouble with the wifi in his office and so he has decided to hardwire all the work stations.

The office consists of a reception desk, the manager Michael’s office, three separate sale’s teams, an accounting department, printer station, lunch room and human resources. The follow network depicts the distance in metres between the work stations.



a) Find the shortest path from the reception to human resources. State the path and the distance.

To hardwire all the workstations, the workstations need to all be connected by cabling.

b) Show span of the cabling on the diagram above and state the minimum amount of cabling needed to complete the job.

The cost of the cabling including labour is approximately $50/metre.

c) How much money do they save by not cabling the lunch room.

**Question Four: [2, 2, 2, 1: 7 marks]**

Consider the following complete bipartite graph.

****

a) Create a matrix to show the weighting of each allocation.

b) Assign tasks A, B, C to 1, 2, 3 in order to maximize the weightings.

c) Assign tasks A, B, C to 1, 2, 3 in order to minimize the weightings

d) What is the difference between the maximum and minimum weightings?

**Question Five: [1, 4, 2, 3: 10 marks]**

The network below represents a system of roads through a major city district. The council has tried to limit the traffic flow through this part of the city and therefor there is only one entry and a single exit point. The arcs on the network represent the roads and the weightings on the arcs give the maximum capacity of cars for that section of road in cars per hour.

a) Label the source and the sink.

b) What is the maximum number of cars that could reach point H per hour given that the only restriction is the capacity of the roads?

b) Show that the maximum flow is equal to the minimum cut.

One of the three roads which currently has a capacity of 20 cars her hour will be upgraded to be able to accommodate a maximum of 60 cars her hour.

c) Describe the effect on the maximum flow for each the roads in question and decide which one they should upgrade, if any.

**Topic: SOLUTIONS**

Time: 45 mins Marks: /45 marks

**No calculator allowed**



**Question One: [4, 2: 6 marks]**

a) Find the maximum flow of the network below.

b) Show that the maximum flow is equal to the minimum cut.

F –H 20

G – I 90

**Question Two: [4, 2, 2, 3, 2: 13 marks]**

Borat is planning his next holiday. Once he has decided that he wants to go on holiday the following things need to happen before he can go.

|  |  |  |  |
| --- | --- | --- | --- |
|  | **Activity** | **Preceding activity** | **Time to complete activity** |
| A | Pick a destination | None | 2 weeks 14 days |
| B | Get relevant vaccinations and health checks | Pick a destination | 3 days |
| C | Apply for passport | Pick a destination | 6 weeks 42 days |
| D | Start saving money | Pick a destination | 81 days |
| E | Apply for a visa | Apply for a passport | 2 weeks 14 days |
| F | Travel insurance | Get relevant vaccinations and health checks | 3 days |
| G | Buy a plane ticket | Start saving | 1 day |
| H | Change currency | Buy a plane ticket | 1 day |
| I | Pack suitcase | Travel insurance, Apply for visa, Change money | 2 days |
| J | Go to the airport and get on plane | Pack suitcase | 1 day |

a) Add the information from the table to the project network below, complete the project network and calculate the number of days Borat allocated to saving money if it takes 100 days before he leaves for his holiday.

 [Note: The diagram below is not drawn to scale] arrows lables and time

b) What is the latest possible day he can start getting his health checks and vaccinations without delaying leaving for his holiday?



The latest day is 91 days after starting.

After deciding where is going to travel to Borat begins collecting donations to take to an orphanage in a village he will visit.

c) How long can be collect donations for without it delaying his departure?



For 86 days

d) If Borat finishes all his relevant health checks on July 14th and uses all the float time allowed for this activity, what date does he go to the airport to get on the plane?

94 days after July 14th – July has 31 days total so 17 days left. Plus August 31 days. Plus September has 30 days. 🡪 78 days

78 + 16 = 94 16th October he goes to the airport.

e) If there is a delay in the processing of his visa application and it takes an extra four weeks to process, how does this affect how long it takes before he can leave for his holiday?

It adds 1 days before he can leave. In reality this delay would cause him to miss his original flight.

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